

# General Certificate of Education June 2010 

Pure Core 2

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## Key to mark scheme and abbreviations used in marking



## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

MPC2

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | $\begin{aligned} & \{\text { Area of sector }=\} \frac{1}{2} r^{2} \theta \\ & \quad=\frac{1}{2} \times 8^{2} \times 1.4=44.8\left\{\mathrm{~m}^{2}\right\} \end{aligned}$ | M1 A1 | 2 | $\frac{1}{2} r^{2} \theta$ seen or used for the area Must be exact, not rounded to |
| (b)(i) | $\begin{aligned} & \{\text { Arc }=\} r \theta \\ & \quad \ldots=11.2 \\ & \text { Perimeter of sector }=16+11.2=27.2\{\mathrm{~m}\} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1F } \end{gathered}$ | 3 | $r \theta$ seen or used for the arc length <br> PI Condone AWRT 11.2 <br> Ft on c's evaluation of $8 \times 1.4$ |
| (ii) | $\begin{gathered} 27.2=2 \pi x \\ x=\frac{27.2}{2 \pi}=4.329 \ldots=4.33 \text { to } 3 \mathrm{sf} \end{gathered}$ | M1 <br> A1 | 2 | [c's numerical answer for (b)(i)] $=2 \pi x$ <br> Condone >3sf |
|  | Total |  | 7 |  |
| 2(a) | $\begin{aligned} & u_{2}=6.8 \\ & u_{3}=8.72 \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1F } \end{gathered}$ | 2 | OE eg 34/5 <br> Ft on $6+0.4 \times$ c's $u_{2}$ |
| (b) | $L=6+0.4 L$ | M1 |  | Replacing $u_{n+1}$ and $u_{n}$ by $L$ |
|  | $L=\frac{6}{1-0.4}$ | m1 |  | PI provided M scored |
|  | $L=10$ | A1 | 3 | Must form an equation in $L$ otherwise $0 / 3$ |
|  | Total |  | 5 |  |

MPC2 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | $6=15$ | M1 |  | Sine rule OE PI |
|  | $\begin{aligned} & \overline{\sin \theta}=\overline{\sin 150} \\ & \sin \theta=\frac{6 \times \sin 150}{15} \quad\{=0.2\} \end{aligned}$ | m1 |  | Rearrangement |
|  | $\theta=11.53(6 . .)=11.5^{\circ}\left\{\text { to nearest } 0.1^{\circ}\right\}$ | A1 | 3 | AG Must see at least 4sf value or an exact value for $\sin \theta(0.2,3 / 15$, OE) before seeing the printed value 11.5 |
| (b) | Angle $B=180-(150+\theta)=18.5$ \{to 3sf $\}$ | B1 |  | Award for $B=$ any value between 18 and 19 inclusive <br> [18.463041....] |
|  | $\text { Area }=\frac{1}{2} \times 6 \times 15 \sin B$ | M1 |  |  |
|  | $=14.3\left\{\mathrm{~cm}^{2}\right\}$ to 3sf | A1 | 3 | Accept a value 14.2 to 14.3 inclusive Note: For methods involving $A C$, for the M1 need both a correct method to find $A C$ and a correct area formula |
|  | Total |  | 6 |  |

MPC2 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4(a) | $p=-3 ; q=3$ | B1;B1 | 2 | Accept even if just embedded in the expansion |
| (b)(i) | $\begin{aligned} & \int\left(1-\frac{1}{x^{2}}\right)^{3} \mathrm{~d} x= \\ & \int\left(1-3 x^{-2}+3 x^{-4}-x^{-6}\right) \mathrm{d} x \end{aligned}$ | M1 |  | Uses (a) with indication of integration and indication of $\frac{1}{x^{n}}=x^{-n}$ PI |
|  | $=x+3 x^{-1}-x^{-3}+\frac{1}{5} x^{-5}\{+c\}$ | m1 <br> A2F,1F | 4 | At least three powers of $x$ correctly obtained <br> Ft on c's non-zero integers $p$ and $q$. A1F if 3 of the 4 terms are correct ( ft ) or if all correct (ft) but left unsimplified Condone missing $+c$. |
| (ii) | $\begin{aligned} & \int_{\frac{1}{2}}^{1}\left(1-\frac{1}{x^{2}}\right)^{3} \mathrm{~d} x= \\ & \left(1+3-1+\frac{1}{5}\right)-\left(\frac{1}{2}+6-8+\frac{32}{5}\right) \end{aligned}$ | M1 |  | Attempting to calculate $\mathrm{F}(1)-\mathrm{F}(1 / 2)$ where $F$ is c's answer to part (b)(i) provided F is not the integrand or the c's equivalent of the integrand $\left(1-\frac{1}{x^{2}}\right)^{3}$. |
|  | $=-\frac{17}{10}$ | A1 | 2 | OE exact answer eg -1.7 |
|  | Total |  | 8 |  |

## MPC2 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a)(i) | $\left\{S_{\infty}=\right\} \frac{a}{1-r}=\frac{10}{1-r}$ | M1 |  | $\frac{a}{1-r} \text { used }$ |
|  | $\frac{10}{1-r}=50 \text { so } 1-r=\frac{10}{50} \Rightarrow r=\frac{4}{5}$ | A1 | 2 | AG Condone verification with the correct final statement but be convinced. |
| (ii) | $\begin{array}{r} 2^{\text {nd }} \text { term }=a r \\ =8 \end{array}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | ar stated or used for the $2^{\text {nd }}$ term. PI by ans ' 8 , |
| (b)(i) | $\begin{aligned} & 4^{\text {th }} \text { term }=a+3 d ; 8^{\text {th }} \text { term }=a+7 d \\ & a+3 d=10, \quad a+7 d=8 \\ & \Rightarrow 4 d=-2 \quad \Rightarrow d=-0.5 \end{aligned}$ | M1 <br> A1F <br> A1 | 3 | Uses $a+(n-1) d$ correctly at least once Both eqns. correct ft on c's (a)(ii) OE eg $8=10+4 d$ OE fraction. |
| (ii) | $a+3(-0.5)=10$ | M1 |  | An appreciation that $a$ is required in (b)(ii) and a valid method to find $a$ anywhere or PI if $a=11.5$ seen/used |
|  |  | AIr |  | Ft on c's non-zero value for $d$ ie using $a=10-3 d$ or $a=$ c's $8-7 d$. [c's 8 is candidate's answer to (a)(ii)] |
|  | $\sum_{n=1}^{40} u_{n}=S_{40}=\frac{40}{2}[2 a+(40-1) d]$ | M1 |  | $\frac{40}{2}[2 a+(40-1) d]$ OE |
|  | $=70$ | A1 | 4 |  |
|  | Total |  | 11 |  |

MPC2 (cont)


MPC2 (cont)


| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 8(a) | ( $y=1$ | B1 | 1 |  |
| (b) | $h=0.2$ | B1 |  | PI |
|  | $\mathrm{f}(\mathrm{x})=2^{4 x}$ |  |  |  |
|  | $\mathrm{I} \approx h / 2\{\ldots\}$ |  |  |  |
|  | $\begin{aligned} & \{.\}=\mathrm{f}(0)+\mathrm{f}(1)+2[\mathrm{f}(0.2)+\mathrm{f}(0.4)+\mathrm{f}(0.6)+\mathrm{f} \\ & (0.8)] \end{aligned}$ | M1 |  | OE summing of areas of the 'trapezia'.. |
|  | $\begin{aligned} & \{.\}=1+16+2\left(2^{0.8}+2^{1.6}+2^{2.4}+2^{3.2}\right) \\ & =1+16+2(1.741 . .+3.031 . .+5.278 . .+9.1 \\ & 895 . .) \quad=[17+2 \times 19.24 . . .] \end{aligned}$ | A1 |  | OE Accept 2dp rounded or truncated evidence |
|  | $\mathrm{I}=5.55$ (to2dp) | A1 | 4 | Must be 5.55 |
| (c) | Stretch(I) in $y$-direction(II) scale | M1 |  | Need (I) and either (II) or (III) |
|  | $\text { factor } \frac{1}{8} \text { (III) }$ | A1 | 2 | Need (I) and (II) and (III) |
|  | ALTn: Translation with an indication that the translation is in the $x$-direction |  |  | Combination of different transformations scores 0/2 |
|  | (B1) $\left[\begin{array}{c} \frac{3}{4} \\ 0 \end{array}\right]$ <br> (B1) |  |  |  |
| (d) | $g(x)=2^{4(x-1)}-\frac{1}{2}$ |  |  | B1 for either $2^{4(x+1)}-\frac{1}{2}$ or for |
|  |  | B2,1,0 |  | $2^{4(x-1)}+\frac{1}{2} \text { or for } 2^{4 x-1}-\frac{1}{2}$ |
| (e)(i) | At $Q, y=0 \Rightarrow 2^{4(x-1)}=2^{-1}$ | M1 |  | Reaches a stage from which linear eqn can be stated directly eg an alternative stage is $4(x-1) \log 2=-\log 2$ |
|  | $\Rightarrow 4 x-4=-1 \Rightarrow x=0.75$ | A1 | 4 | NMS mark as 4 or 0 |
|  | $\log _{a} k=\log _{a} 2^{3}+\log _{a} 5-\log _{a} 4$ | M1 |  | One law of logs used |
|  | $\log _{a} k=\log _{a}\left(2^{3} \times 5\right)-\log _{a} 4$ |  |  | A second law of logs used; could be |
|  |  | M1 |  | $\log _{a} k=\log _{a} 2^{3}+\log _{a}\left(\frac{3}{4}\right)$ |
|  | $\log _{a} k=\log _{a}\left(\frac{2^{3} \times 5}{4}\right)=\log _{a} 10 \Rightarrow k=1$ | A1 | 3 | CSO AG |
| (ii) | $2^{4 x-3}=\frac{5}{4} \text { so }$ |  |  | Equate $y$ 's, take logs (to any base) of both sides and apply $3^{\text {rd }}$ law of logs. |
|  | $(4 x-3) \log _{10} 2=\log _{10} \frac{5}{4}$ | M1 |  | $\text { Altn } 4 \times \log 2=\log \left(\frac{5}{4} \times 2^{3}\right)$ |
|  | $3 \log _{10} 2+\log _{10}\left(\frac{5}{4}\right)$ |  |  | Rearrange correctly to $x=\ldots$. <br> Altn $4 x \log 2=\log 10$ |
|  | $x=4 \log _{10} 2$ |  |  | In both cases, log term(s) must have same base and expressions must be in |
|  | $x=\frac{\log _{10} 10}{4 \log _{10} 2} \quad \text { so } \quad x=\frac{1}{4 \log _{10} 2}$ | m1 <br> A1 | 3 | an exact form, ie not approx. dec. vals CSO AG Must be clear evidence that base 10 is used, also be convinced |
|  | Total |  | 17 |  |
|  | TOTAL |  | 75 |  |

